

$$\mathbf{x} = \mathbf{x}_f - \mathbf{x}_i \quad \Delta \mathbf{v} = \mathbf{v}_f - \mathbf{v}_i$$

$$= \frac{\Delta \vec{r}}{\Delta t} \quad \vec{a} = \frac{\Delta \vec{v}}{\Delta t}$$

$$v = |\mathbf{v}| = \sqrt{v_x^2 + v_y^2}$$

$$\theta = \tan^{-1}\left(\frac{v_y}{v_x}\right)$$



$$\omega = \frac{\Delta \theta}{\Delta t} \quad \alpha = \frac{\Delta \omega}{\Delta t}$$

$$= \mathbf{v}_0 + \mathbf{a}t$$

$$= \mathbf{x}_0 + \mathbf{v}_0 t + \frac{1}{2} \mathbf{a} t^2$$

$$-v_o^2 = 2a(x - x_0)$$

$$= \frac{v_f^2 - v_i^2}{2a}$$

Data Visualization

$$\omega = 2\pi f \quad f = \frac{1}{T}$$

$$\omega = \omega_0 + \alpha t$$

$$\theta = \theta_0 + \omega_0 t + \frac{1}{2} \alpha t^2$$

$$\omega_0^2 = 2\alpha(\theta - \theta_0)$$

Curvefit Rankings for 0.5% SEV CO₂

Rank	F-statistic
1	7.962883557
2	7.8601110639
3	7.5283512645
4	7.3357010958
5	6.3801158367
6	3.8079206858
7	3.742891358
8	3.5727028219
9	3.5546937052
10	3.0133372321
11	2.7408796673
12	2.6986270263
13	2.5801276758
14	2.5622800357
15	2.1798855221

Prof. Dr. Javier Valdes
Javier.valdes@th-deg.de

IAI - Institut für Angewandte Informatik
 Institute for Applied Informatics

Technische Hochschule Deggendorf
 Technologie Campus Freyung
 Grafenauer Str. 22, D- 94078 Freyung,
 Germany

Tel.: +49 8551 91764 40
 Fax: +49 8551 91764 69

$$x = A \cos(\omega t + \phi) \quad v = -A \omega \sin(\omega t + \phi)$$

Example of Exploratory data Analysis (Peng)



1. Characteristics of exploratory graphs

The goal of making exploratory graphs is usually developing a **personal understanding of the data** and to prioritize tasks for follow up. Details like axis orientation or legends, while present, are generally cleaned up and prettified if the graph is going to be used for communication later. Often color and plot symbol size are used to convey various dimensions of information.

2 Air Pollution in the United States

In this notebook the key question we are interested is: **Are there any counties in the U.S. that exceed the national standard for fine particle pollution?** This question has important consequences because counties that are found to be in violation of the national standards can face serious legal consequences. In particular, states that have counties in violation of the standards are required to create a State Implementation Plan (SIP) that shows how those counties will come within the national standards within a given period of time.



Exploratory analysis: Who, what, and how

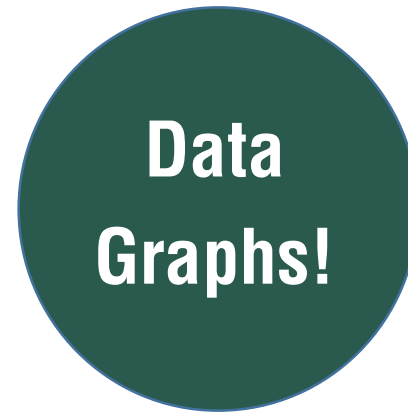
Who:



What

**Action
Mechanism
Tone**

How



Example: Vaccination

Who: The budget committee that can approve funding for continuation of the winter vaccination program.

What: The vaccination program was a success; please approve budget of \$X to continue.

How: illustrate success with data collected through the survey conducted before and after the pilot program.

neu

Field Application Scientist

Curiox Biosystems

Frankfurt am Main • Vorübergehend im Homeoffice

3.500 € pro Monat

Anforderungen

Bachelor's

➤ Jetzt direkt bewerben

- Key applications include: life science research, immunology, immunotherapy, drug discovery diagnostics, cell therapy research and manufacturing.

vor 4 Tagen • [Job speichern](#) • [mehr...](#)



Exploratory analysis: Who, what, and how

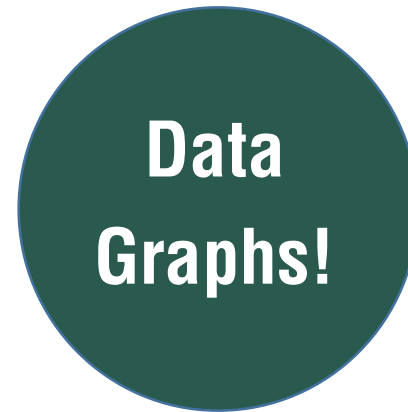
Who:



What

**Action
Mechanism
Tone**

How



Example: Vaccination

Who: The budget committee that can approve funding for continuation of the winter vaccination program.

What: The vaccination program was a success; please approve budget of \$X to continue.

How: illustrate success with data collected through the survey conducted before and after the pilot program.

neu

Field Application Scientist

Curiox Biosystems

Frankfurt am Main • Vorübergehend im Homeoffice

3.500 € pro Monat

Anforderungen

Bachelor's

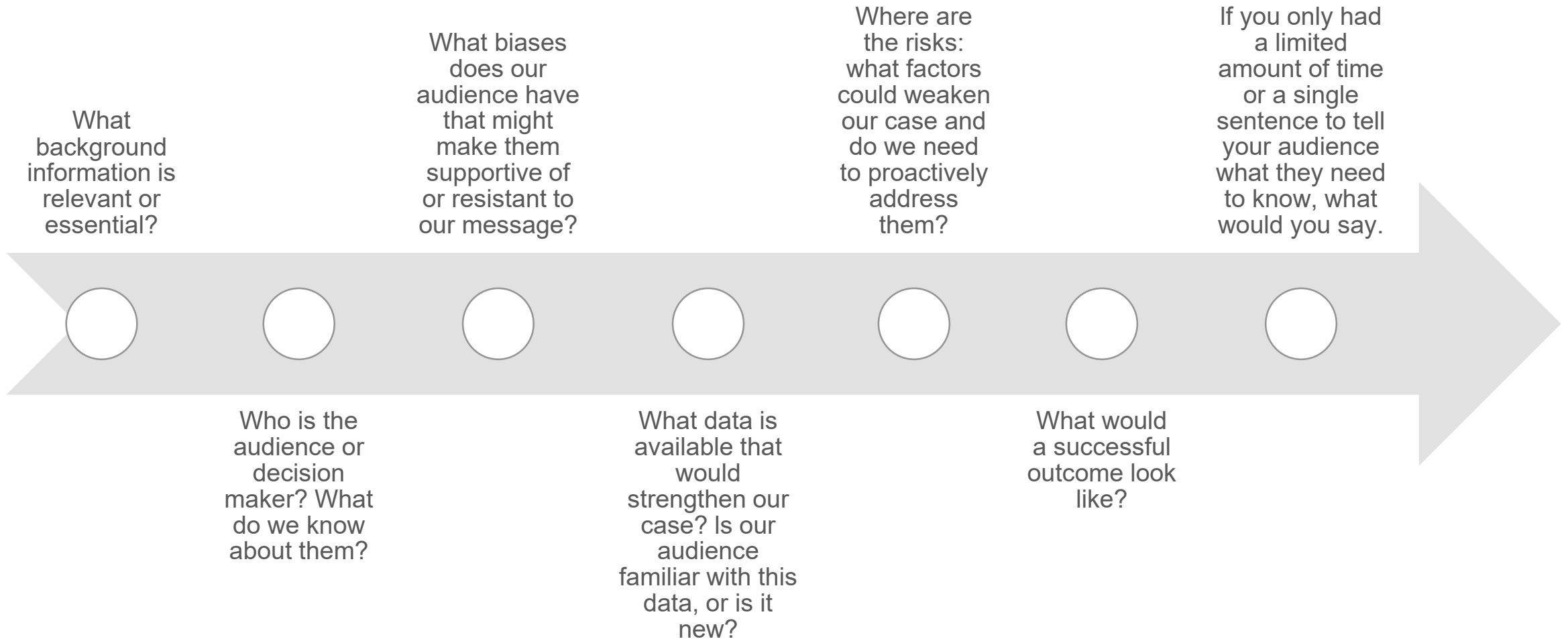
➤ Jetzt direkt bewerben

- Key applications include: life science research, immunology, immunotherapy, drug discovery diagnostics, cell therapy research and manufacturing.

vor 4 Tagen • [Job speichern](#) • [mehr...](#)



Exploratory analysis: Who, what, and how





Exploratory analysis: Who, what, and how

3-minute story

Imagine you are a Field Application Scientist. You just wrapped up an experimental pilot that was aimed at reducing exposure to Influenza in a nursing home. You surveyed the old age persons at the onset and end of the program to understand whether and how perceptions toward vaccination changed. You believe the data shows a great success story. You would like to expand the use of your methodology in other nursing homes to gather more data.



Exploratory analysis: Who, what, and how

3-minute story

Who?

The call to action would be different for the different groups

What?

Show before & after survey data to demonstrate success of program

How?

Data collected via survey at the onset and end of the program



Exploratory analysis: Who, what, and how

3-minute story

Issue:

Elderly people have bad attitudes about vaccination

Demonstrate Issue:

Show Elderly population rates over the course of last campaigns

Ideas for overcoming issue, including developing pilot program

Describe pilot program-goals, structure etc.

Show before & after survey data to demonstrate success of program

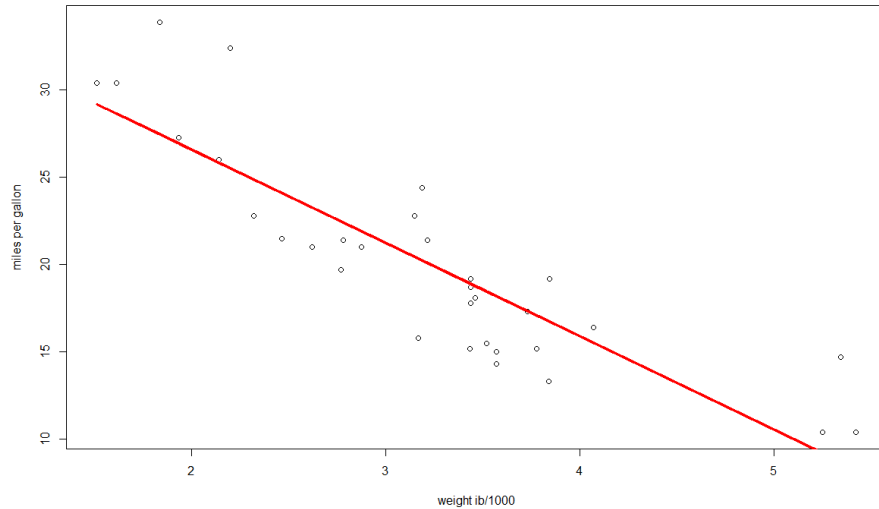
RECOMMENDATION:
Pilot was a success, let's expand it we need \$\$



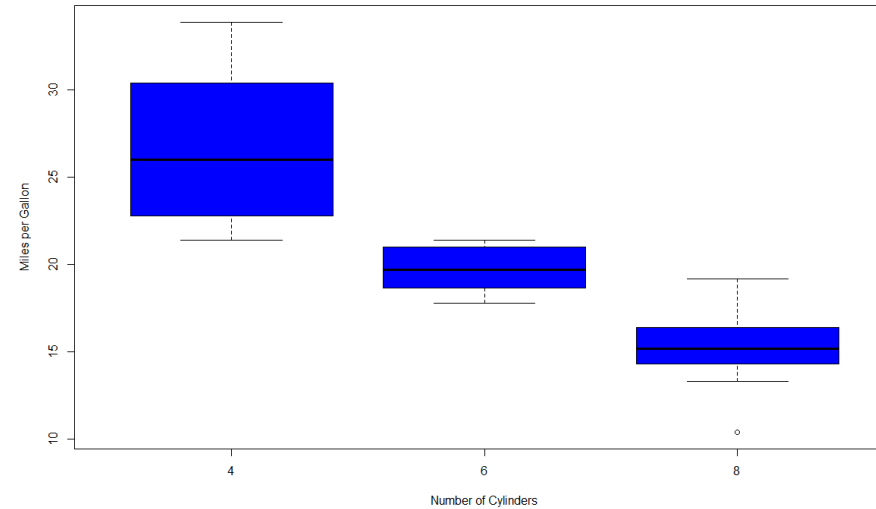
Exploratory analysis: Who, what, and how

3-minute story

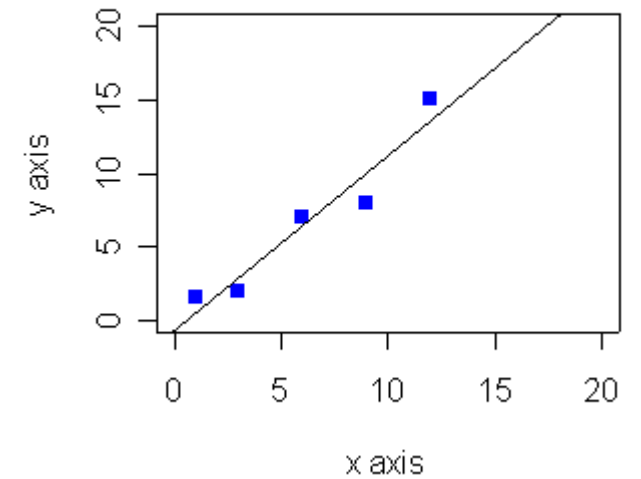
weight vs miles per gallon



Cylinders vs. MPG



my plot



Why investing on visual information?



How many P's can you find in the text?

A M C D F G O I S H P O F Q H O P I U O I U L F K S D K

F K F J Z F C P T H B M U G I N D I C A T O R S D H D X

B E W Z C O M P O S I T E A E T F R J L M N O J K P B R

L A D X O G F J E I L K S A P R P U E D G H M X O Q B I

Effective communication through visualization



How many P's can you find in the text?

A M C D F G O I S H P O F Q H O P I U O I U L F K S D K
F K F J Z F C P T H B M U G I N D I C A T O R S D H D X
B E W Z C O M P O S I T E A E T F R J L M N O J K P B R
L A D X O G F J E I L K S A P R P U E D G H M X O Q B I

Effective communication through visualization



Article

Talk

Read

Edit

View history

Search Wikipedia



Principles of grouping

From Wikipedia, the free encyclopedia



This article has multiple issues. Please help **improve it** or discuss these issues on the **talk page**. *(Learn how and when to [hide]*

remove these template messages)

- This article **needs additional citations for verification**. *(December 2018)*
- This article **needs attention from an expert in Cognitive science**. *(April 2011)*

The **principles of grouping** (or **Gestalt laws of grouping**) are a set of principles in [psychology](#), first proposed by [Gestalt psychologists](#) to account for the observation that humans naturally perceive objects as organized patterns and objects, a principle known as [Prägnanz](#). Gestalt psychologists argued that these principles exist because the mind has an innate disposition to perceive patterns in the stimulus based on certain rules. These principles are organized into five categories: Proximity, Similarity, Continuity, Closure, and Connectedness.^{[1][2][3][4]}

[Irvin Rock](#) and Steve Palmer, who are acknowledged as having built upon the work of [Max Wertheimer](#) and others and to have identified additional grouping principles,^[5] note that Wertheimer's laws have come to be called the "Gestalt laws of grouping" but state that "perhaps a more appropriate description" is "principles of grouping."^{[6][7]} Rock and Palmer helped to further Wertheimer's research to explain human perception of groups of objects and how *whole* objects are formed from *parts* which are perceived.

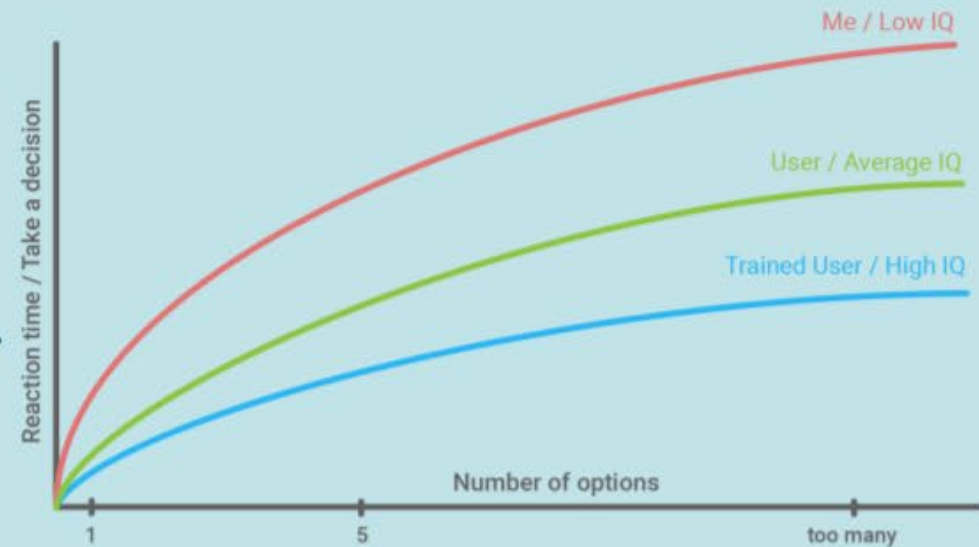
Contents [\[hide\]](#)

1 [Proximity](#)

Effective communication through visualization



- Gestalt psychology
- Miller's law – The number of objects an average person can hold in working memory is about seven [Also known as the magical number Seven, plus or minus two]
- Hick's law – Describes the time it takes for a person to make a decision as a result of the possible choices available: Increasing the number of choices will increase the decision time logarithmically



Effective communication through visualization



Emergence – forming complex patterns from simple rules.



Can you see the cow?

Visual perception and the Principles of Gestalt



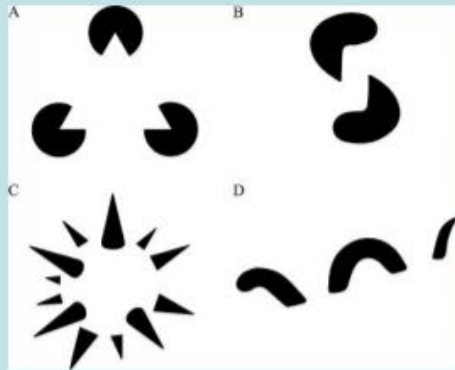
Emergence – forming complex patterns from simple rules.



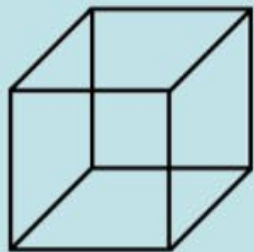
Pragnanz – Simplicity is the key



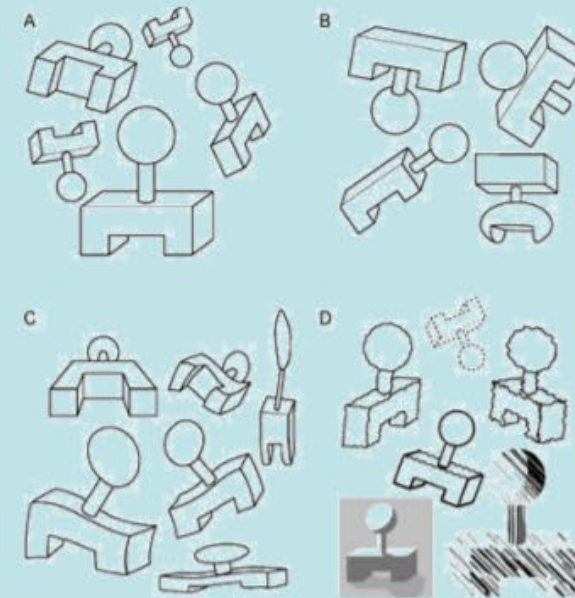
- **Reification** - The perceived experience contains more information than the sensorial stimulus.



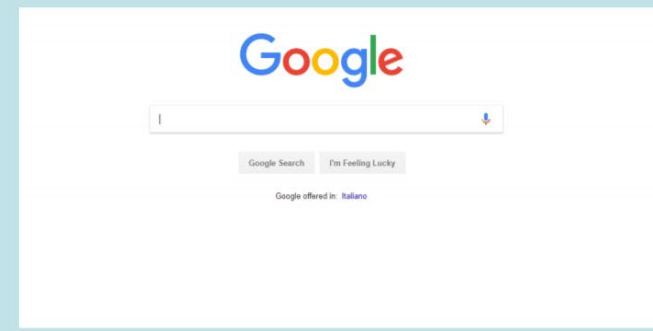
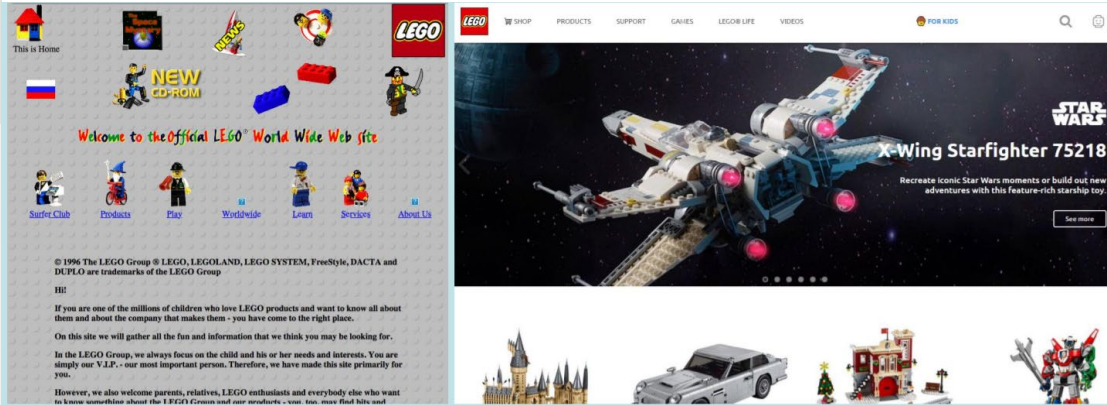
- **Multistability** - Ambiguous perceptual experiences to pop back and forth between alternative interpretations.



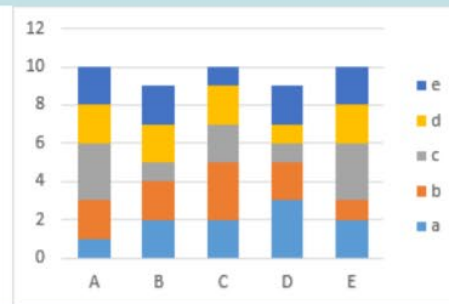
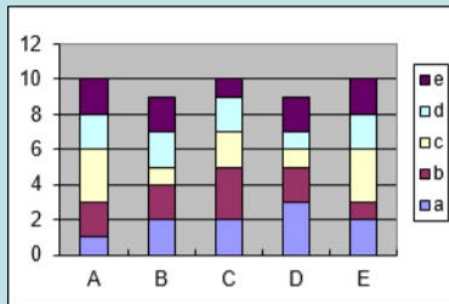
- **Invariance** - Simple objects are recognized independent of rotation, translation and scale.



Pragnanz – Simplicity is the key



Excel 2003 vs Excel 2013



$$\text{Data-Ink ratio} = \frac{\text{data-ink}}{\text{total ink used to make the graphic}}$$

= 1 – proportion of a graphic that can be erased without loss of data-information

(Tufte, Edward – *The visual display of quantitative information*)

Some suggestions to reduce data-ink ratio:

- No 3d charts
- No backgrounds, shadows or gradients
- Remove gridlines, decoration, borders, fillcolors

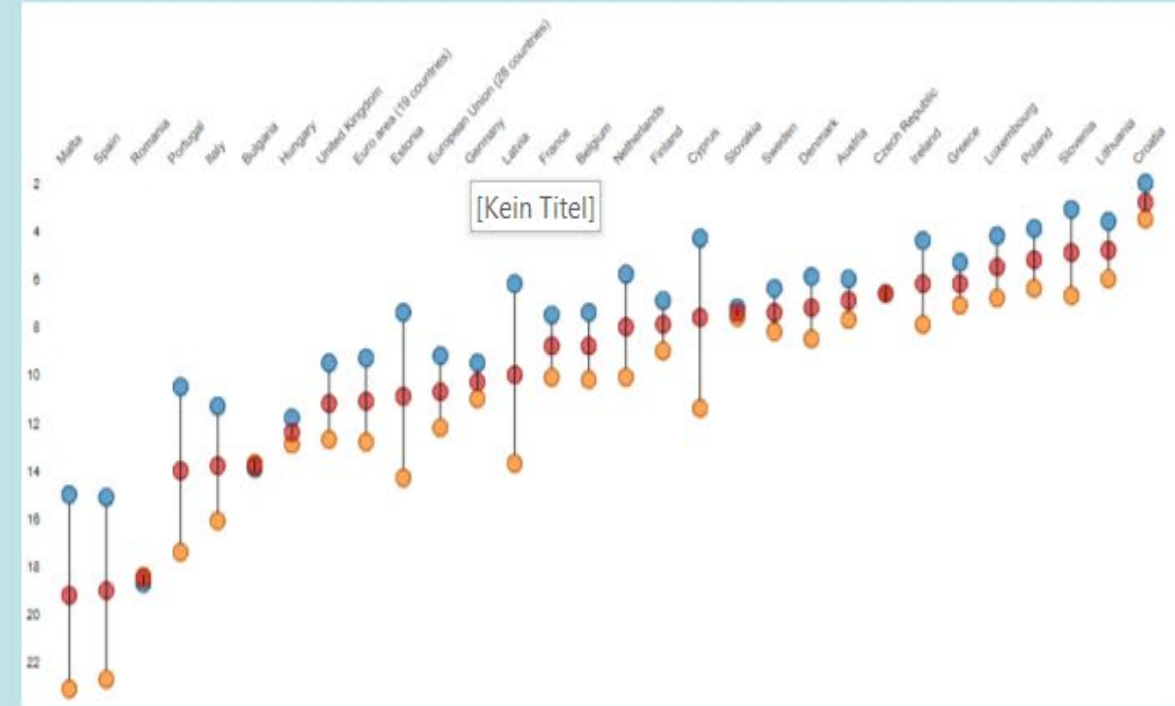
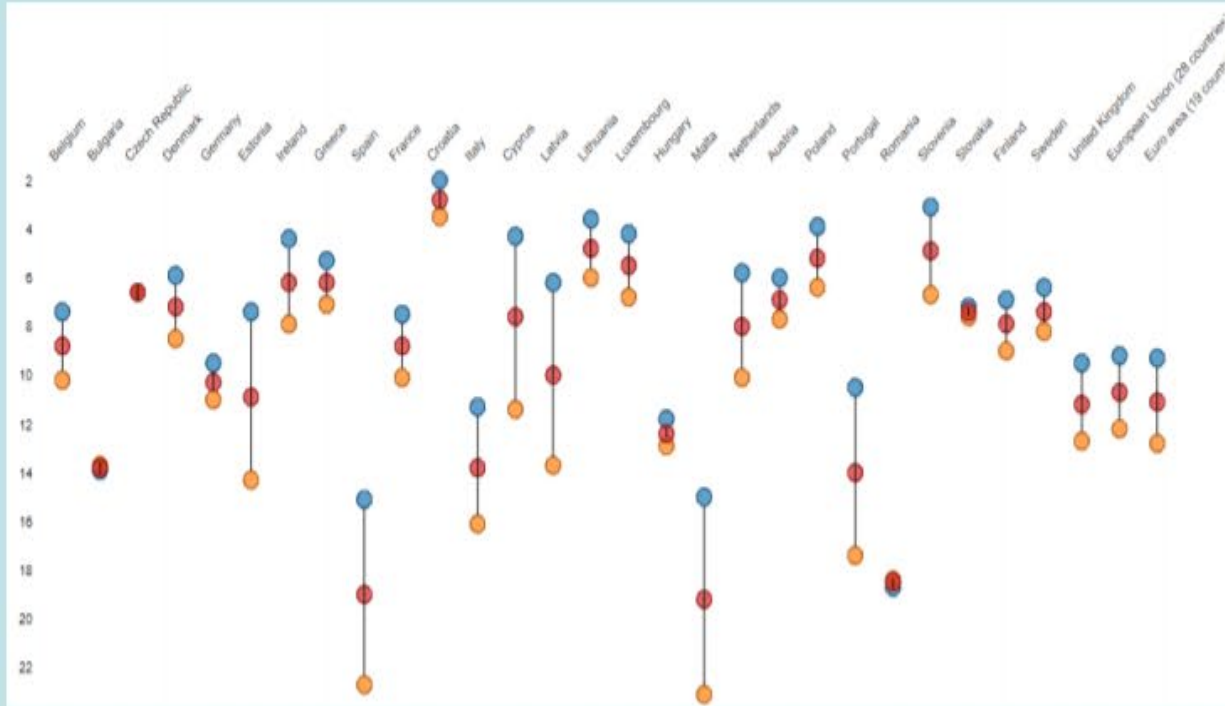
Effective communication through visualization



What can be removed from a chart while keeping the information?



Effective communication through visualization



Gestalt principles



- **Law of Simplicity** — Our eyes seek simplicity in complex shapes, preventing us from being overwhelmed by information overload.
- **Law of Proximity** — We perceive objects close to each other as belonging to a group.
- **Law of Similarity** — We seek similarities and differences and link similar items into a group.
- **Law of Figure and Ground** — We tend to segment our visual world into figure and ground. The figure is the object in the focus of our vision, and the ground is the background.
- **Law of Focal Point** — Whatever stands out visually will be given higher attention.

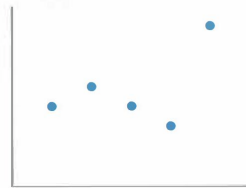
<https://medium.com/nightingale/how-to-apply-gestalt-psychology-principles-in-data-visualization-6242f4f1a3de>

Choosing an effective visual

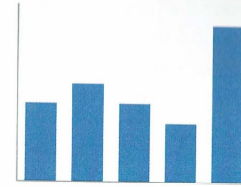


91%

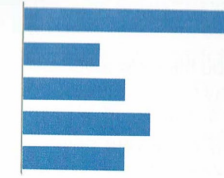
Simple text



Scatterplot



Vertical bar



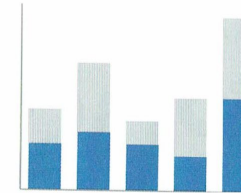
Horizontal bar

	A	B	C
Category 1	15%	22%	42%
Category 2	40%	36%	20%
Category 3	35%	17%	34%
Category 4	30%	29%	26%
Category 5	55%	30%	58%
Category 6	11%	25%	49%

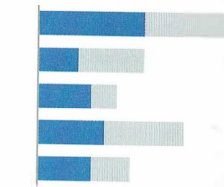
Table



Line



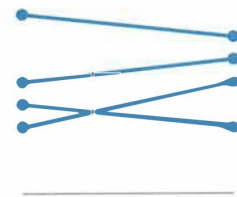
Stacked vertical bar



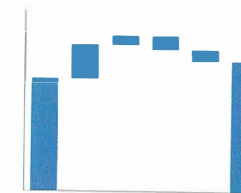
Stacked horizontal bar

	A	B	C
Category 1	15%	22%	42%
Category 2	40%	36%	20%
Category 3	35%	17%	34%
Category 4	30%	29%	26%
Category 5	55%	30%	58%
Category 6	11%	25%	49%

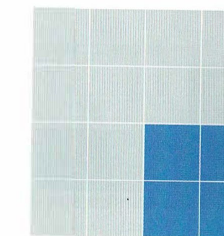
Heatmap



Slopegraph



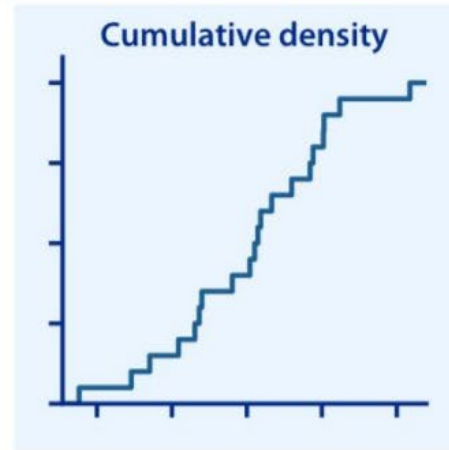
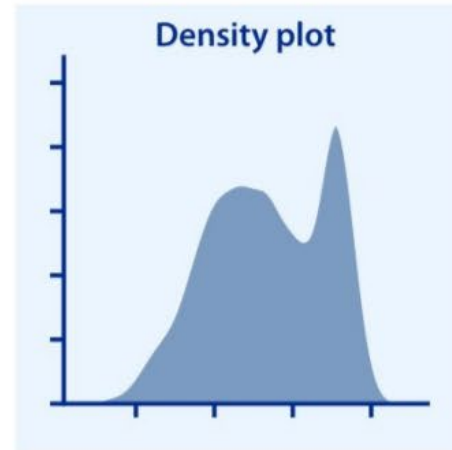
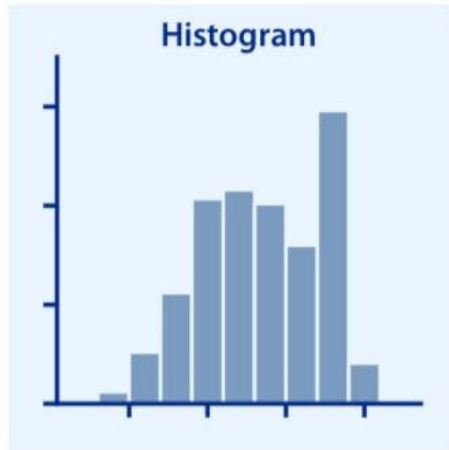
Waterfall



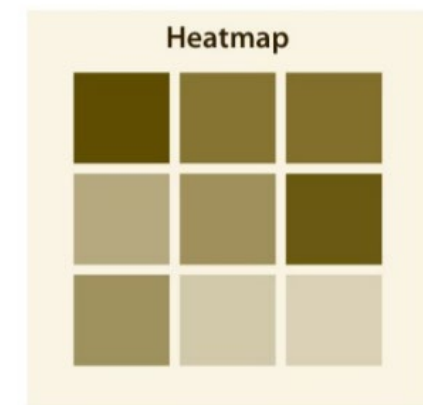
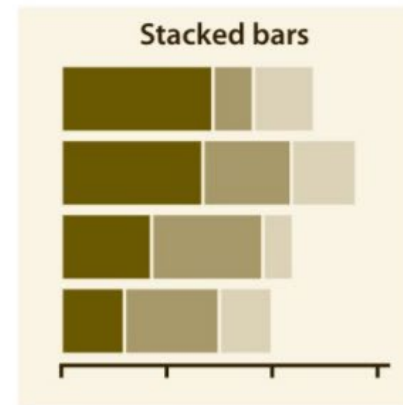
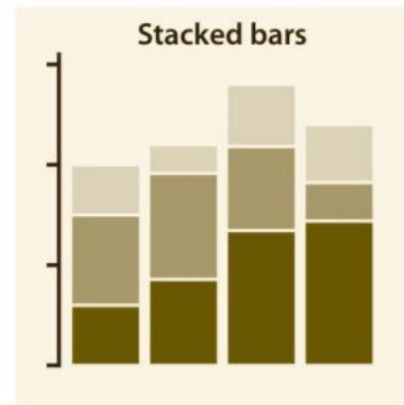
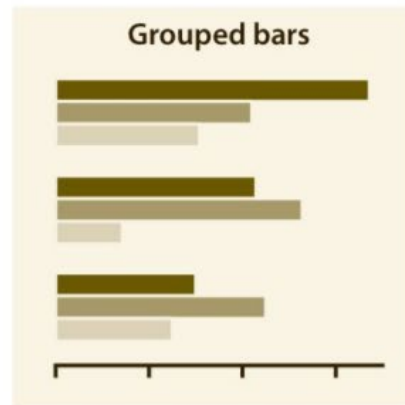
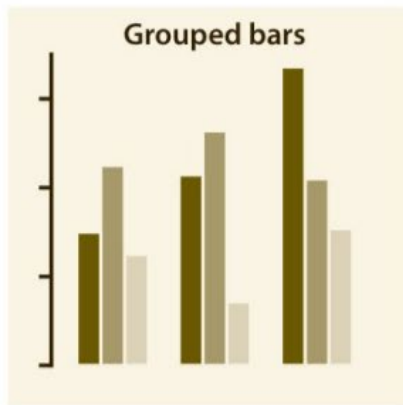
Square area



Distributions

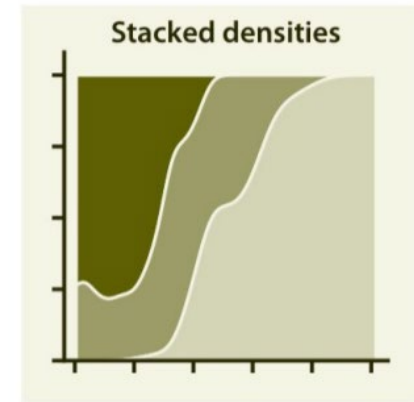
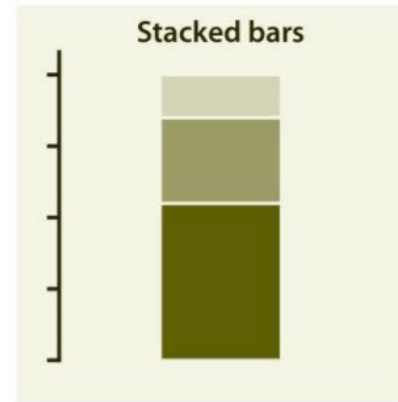
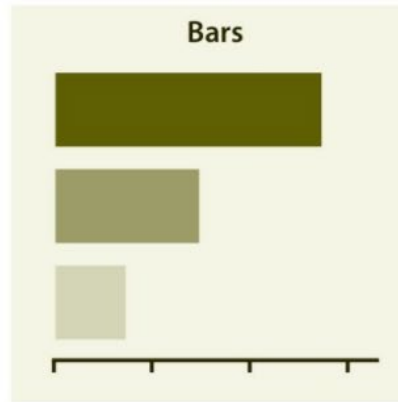
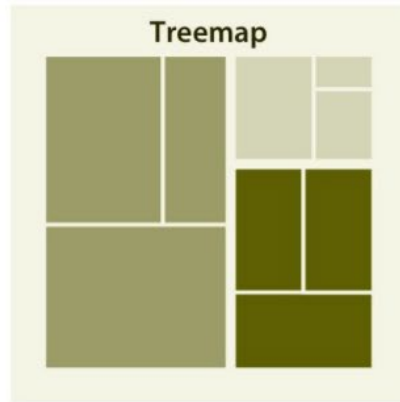
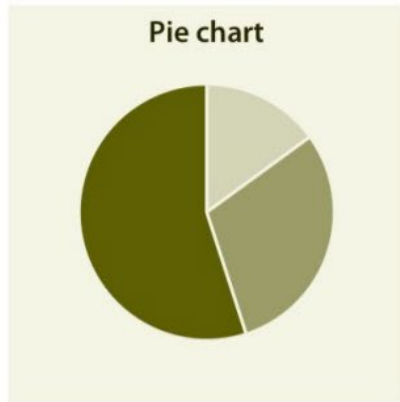


Comparisons

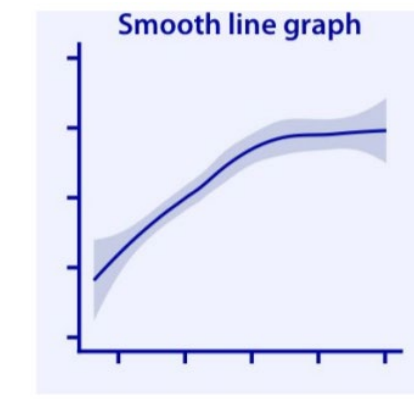
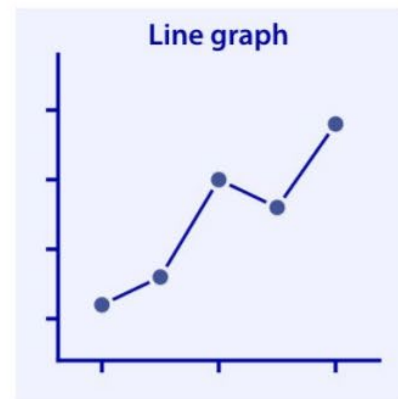
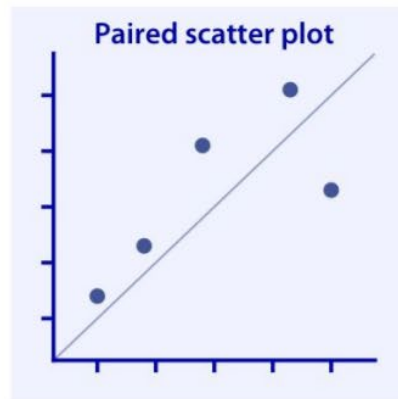
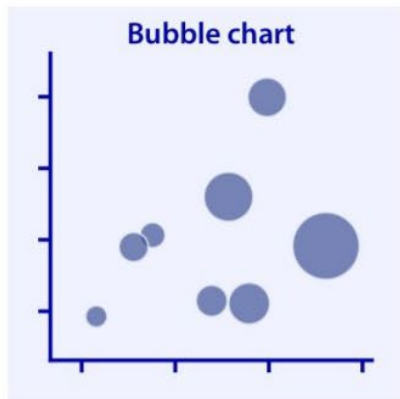
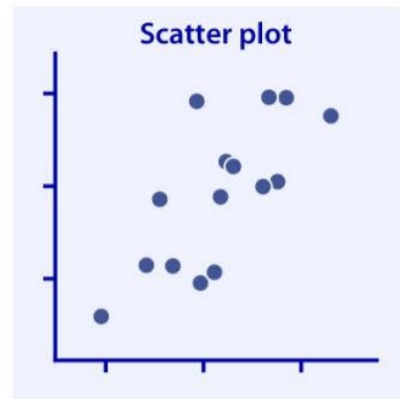




Proportions



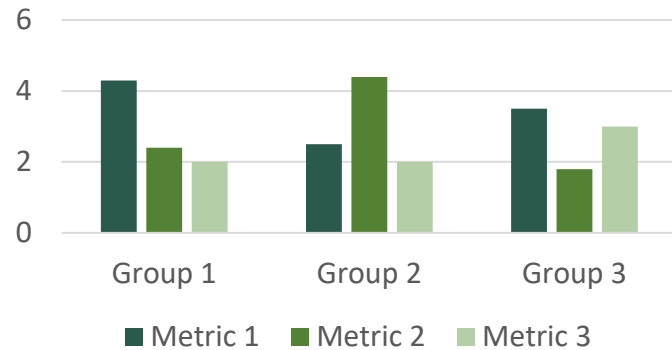
x-y relationships



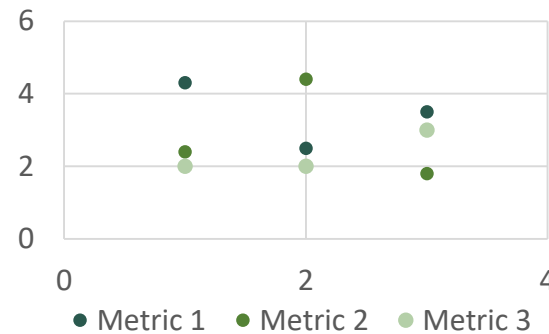
Graphs



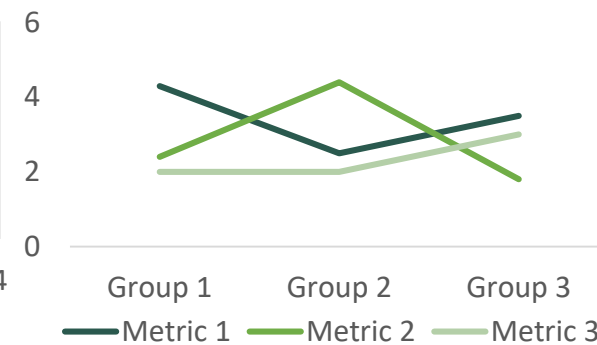
Bars graph



Points



Lines



Area



1

While tables interact with our verbal system, **graphs interact with our visual system**, which is **faster** at **processing** information.

2

The types of graphs frequently use fall into **four categories**: points, lines, bars, and area.

3

Note:

there are a plethora of graph types out there, we will cover the **most common**.



Simple text:

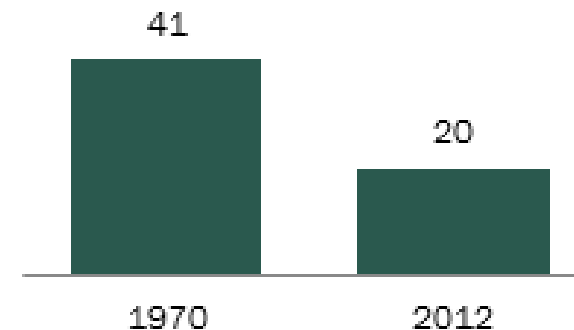
20%

Of children had a **traditional stay-at-home mom** in 2012, compared to 41% in 1970

FIGURE 2.1 Stay-at-home text simple text makeover

Children with a “Traditional” Stay-at-Home Mother

% of children with a married stay-at-home mother with a working husband



Note: Based on children younger than 18. Their mothers are categorized based on employment status in 1970 and 2012.

Source: Pew Research Center analysis of March Current Population Surveys Integrated Public Use Microdata Series (IPUMS-CPS), 1971 and 2013

PEW RESEARCH CENTER

Tables



Heavy borders

Group	Metric A	Metric B	Metric C
Group 1	\$X.X	Y%	Z.ZZZ
Group 2	\$X.X	Y%	Z.ZZZ
Group 3	\$X.X	Y%	Z.ZZZ
Group 4	\$X.X	Y%	Z.ZZZ
Group 5	\$X.X	Y%	Z.ZZZ

Light borders

Group	Metric A	Metric B	Metric C
Group 1	\$X.X	Y%	Z.ZZZ
Group 2	\$X.X	Y%	Z.ZZZ
Group 3	\$X.X	Y%	Z.ZZZ
Group 4	\$X.X	Y%	Z.ZZZ
Group 5	\$X.X	Y%	Z.ZZZ

Minimal borders

Group	Metric A	Metric B	Metric C
Group 1	\$X.X	Y%	Z.ZZZ
Group 2	\$X.X	Y%	Z.ZZZ
Group 3	\$X.X	Y%	Z.ZZZ
Group 4	\$X.X	Y%	Z.ZZZ
Group 5	\$X.X	Y%	Z.ZZZ

1

Tables

are great to communicating to a **mixed audience** whose members will each look for their **particular row** of interest

2

The **data** should be what stands out, **not the borders.**

3

Note:

Using a table in a live presentation is **rarely** a good idea.

Tables



Heavy borders

Group	Metric A	Metric B	Metric C
Group 1	\$X.X	Y%	Z.ZZZ
Group 2	\$X.X	Y%	Z.ZZZ
Group 3	\$X.X	Y%	Z.ZZZ
Group 4	\$X.X	Y%	Z.ZZZ
Group 5	\$X.X	Y%	Z.ZZZ

Light borders

Group	Metric A	Metric B	Metric C
Group 1	\$X.X	Y%	Z.ZZZ
Group 2	\$X.X	Y%	Z.ZZZ
Group 3	\$X.X	Y%	Z.ZZZ
Group 4	\$X.X	Y%	Z.ZZZ
Group 5	\$X.X	Y%	Z.ZZZ

Minimal borders

Group	Metric A	Metric B	Metric C
Group 1	\$X.X	Y%	Z.ZZZ
Group 2	\$X.X	Y%	Z.ZZZ
Group 3	\$X.X	Y%	Z.ZZZ
Group 4	\$X.X	Y%	Z.ZZZ
Group 5	\$X.X	Y%	Z.ZZZ

**Tables
work best
when...**

Used to **look** up individual values

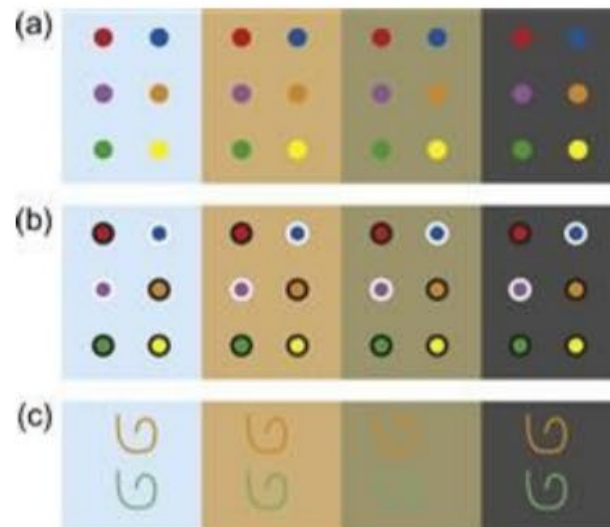
Used to **compare** individual values

Data must be **precise**

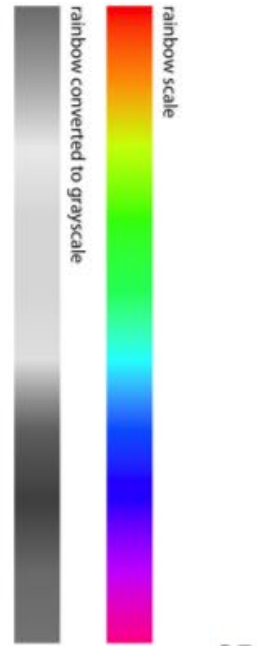
You must include **multiple** units of **measure**

You wish to show both **details** and their **sums**

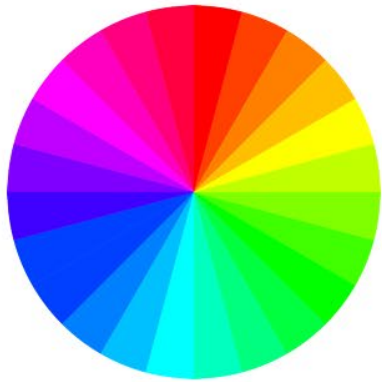
Effective communication through visualization



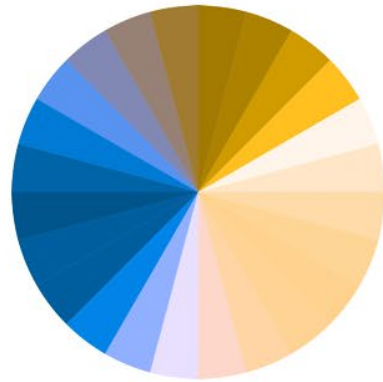
- You need different palettes for continuous, divergent, and discrete data.
- 10 colors **max** for reliable differentiation
- Vary your palette in hue **and** brightness.



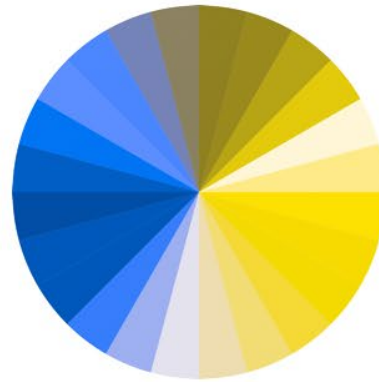
Effective communication through visualization



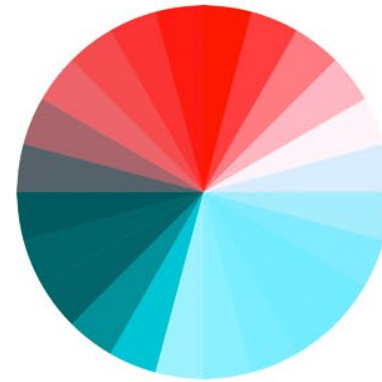
Regular vision



Deuteranopia



Protanopia



Tritanopia



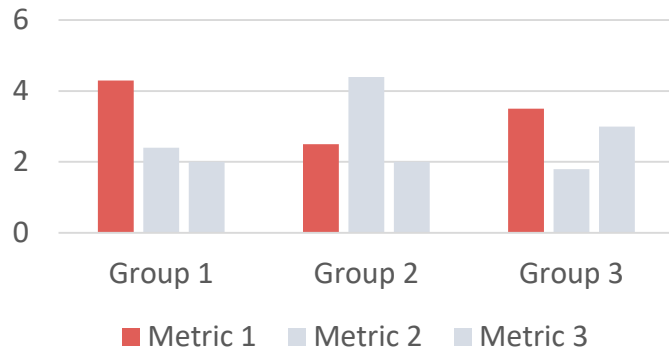
Monochromacy



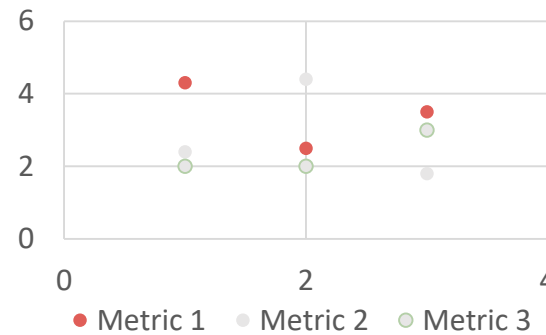
Graphs



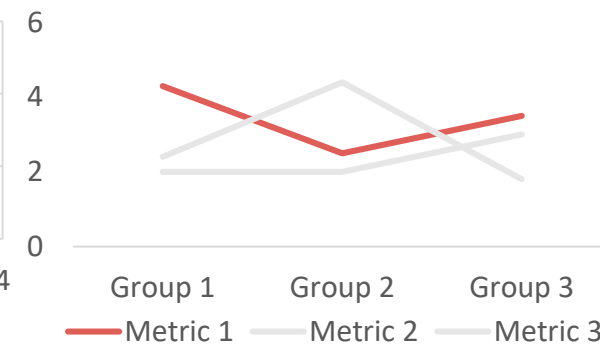
Bars graph



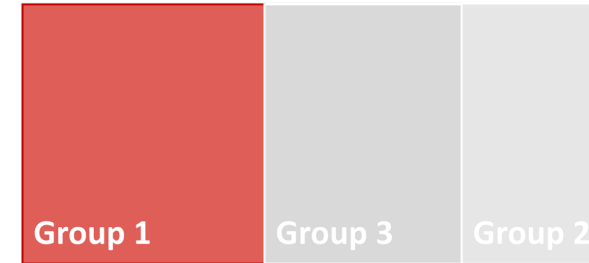
Points



Lines



Area



1

While tables interact with our verbal system, **graphs interact with our visual system**, which is **faster** at **processing** information.

2

The types of graphs frequently use fall into **four categories**: points, lines, bars, and area.

3

Note: there are a plethora of graph types out there, we will cover the **most common**.



Plotting with ggplot2

The **concept** behind **ggplot2** divides plot into three (even more) different **fundamental** parts:
Plot = data + Aesthetics + Geometry

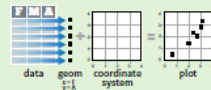
- **data** is a data frame
- **Aesthetics** is used to indicate x and y variables. It can also be used to control the **color**, the **size** or the **shape** of points, the height of bars, etc.....
- **Geometry** defines the type of graphics (histogram, box plot, line plot, density plot, dot plot,)
- All the rest....

Data Visualization with ggplot2 Cheat Sheet

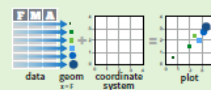


Basics

ggplot2 is based on the **grammar of graphics**, the idea that you can build every graph from the same components: a **data set**, a **coordinate system**, and **geoms**—visual marks that represent data points.



To display values, map variables in the data to visual properties of the geom (**aesthetics**) like **size**, **color**, and **x** and **y** locations.



Complete the template below to build a graph.

```
ggplot(data = <DATA>) +
  <GEOM_FUNCTION>
  mapping = aes(<MAPPINGS>),
  stat = <STAT>,
  position = <POSITION>
  +
  <COORDINATE_FUNCTION> +
  <FACET_FUNCTION> +
  <SCALE_FUNCTION> +
  <THEME_FUNCTION>
```

ggplot(data = mpg, aes(x = cty, y = hwy))
Begins a plot that you finish by adding layers to. Add one geom function per layer.

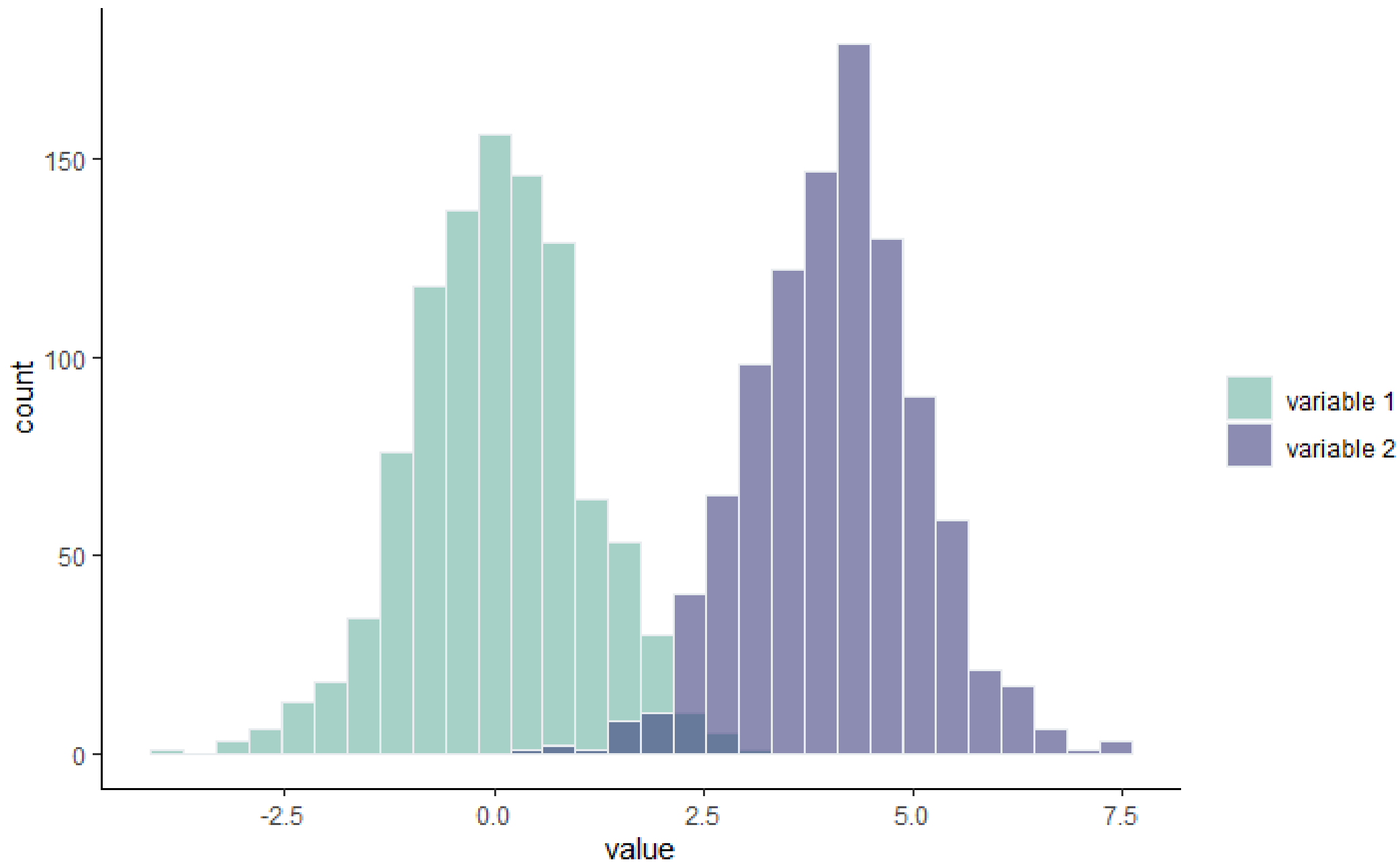
qplot(x = cty, y = hwy, data = mpg, geom = "point")
Creates a complete plot with given data, geom, and mappings. Supplies many useful defaults.

last_plot()
Returns the last plot

ggsave("plot.png", width = 5, height = 5)
Saves last plot as 5" x 5" file named "plot.png" in working directory. Matches file type to file extension.

Geoms - Use a geom function to represent data points, use the geom's aesthetic properties to represent variables. Each function returns a layer.

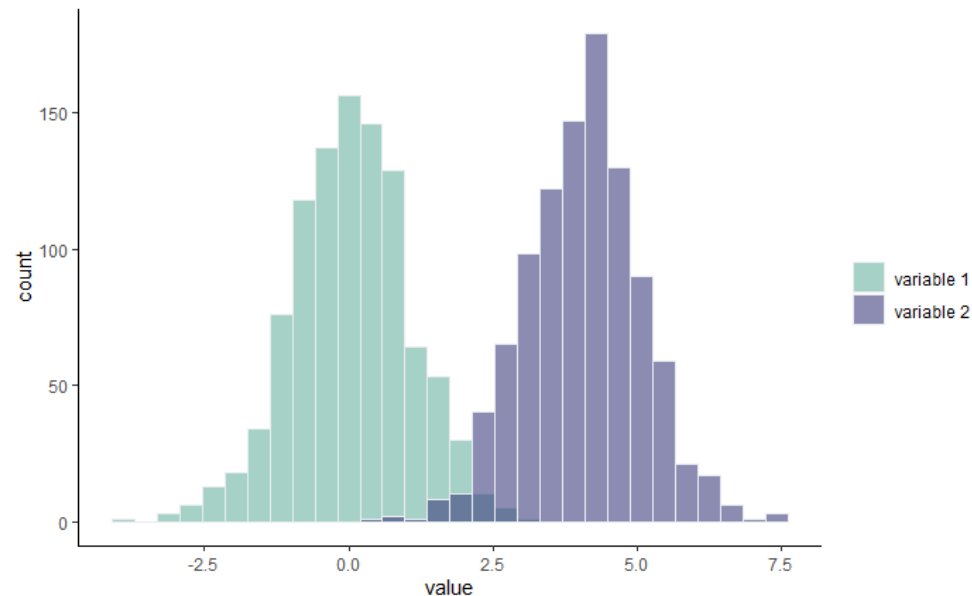
Graphical Primitives	Two Variables
<p>a <- ggplot(economics, aes(date, unemployment)) b <- ggplot(seals, aes(x = long, y = lat)) (Useful for expanding limits)</p> <p>a + geom_blank() (Useful for expanding limits)</p> <p>b + geom_curve(aes(yend = lat + 1, xend = long + 1, curvature = z)) - x, xend, y, yend, alpha, angle, color, curvature, linetype, size</p> <p>a + geom_path(lineend = "butt", linejoin = "round", linemitre = 1) x, y, alpha, color, group, linetype, size</p> <p>a + geom_polygon(aes(group = group)) x, y, alpha, color, fill, group, linetype, size</p> <p>b + geom_rect(aes(xmin = long, ymin = lat, xmax = long + 1, ymax = lat + 1)) - xmin, xmax, ymax, ymin, alpha, color, fill, linetype, size</p> <p>a + geom_ribbon(aes(ymin = unemployment - 900, ymax = unemployment + 900)) - x, ymax, ymin, alpha, color, fill, group, linetype, size</p>	<p>Continuous X, Continuous Y e <- ggplot(mpg, aes(cty, hwy))</p> <p>e + geom_label(aes(label = cty), nudge_x = 1, nudge_y = 1, check_overlap = TRUE) x, y, label, alpha, angle, color, family, fontface, hjust, lineheight, size, vjust</p> <p>e + geom_jitter(height = 2, width = 2) x, y, alpha, color, fill, shape, size</p> <p>e + geom_point() x, y, alpha, color, fill, shape, size, stroke</p> <p>e + geom_quantile() x, y, alpha, color, group, linetype, size, weight</p> <p>e + geom_rug(sides = "bl") x, y, alpha, color, linetype, size</p> <p>e + geom_smooth(method = lm) x, y, alpha, color, fill, group, linetype, size, weight</p> <p>e + geom_text(aes(label = cty), nudge_x = 1, nudge_y = 1, check_overlap = TRUE) x, y, label, alpha, angle, color, family, fontface, hjust, lineheight, size, vjust</p>
<p>Line Segments common aesthetics: x, y, alpha, color, linetype, size</p> <p>b + geom_abline(aes(intercept = 0, slope = 1)) b + geom_hline(aes(yintercept = lat)) b + geom_vline(aes(xintercept = long)) b + geom_segment(aes(yend = lat + 1, xend = long + 1)) b + geom_spoke(aes(angle = 1:1155, radius = 1))</p>	<p>Continuous Bivariate Distribution h <- ggplot(diamonds, aes(carat, price))</p> <p>h + geom_bin2d(binwidth = c(0.25, 500)) x, y, alpha, color, fill, linetype, size, weight</p> <p>h + geom_density2d() x, y, alpha, colour, group, linetype, size</p> <p>h + geom_hex() x, y, alpha, colour, fill, size</p> <p>Continuous Function i <- ggplot(economics, aes(date, unemployment))</p> <p>i + geom_area() x, y, alpha, color, fill, linetype, size</p> <p>i + geom_line() x, y, alpha, color, group, linetype, size</p> <p>i + geom_step(direction = "hv") x, y, alpha, color, group, linetype, size</p> <p>Visualizing error df <- data.frame(grp = c("A", "B"), fit = 4:5, se = 1:2) j <- ggplot(df, aes(grp, fit, ymin = fit - se, ymax = fit + se))</p> <p>j + geom_crossbar(fatten = 2) x, y, ymax, ymin, alpha, color, fill, group, linetype, size</p> <p>j + geom_errorbar() x, ymax, ymin, alpha, color, group, linetype, size, width (also geom_errorbarh())</p> <p>j + geom_linerange() x, ymin, ymax, alpha, color, group, linetype, size</p> <p>j + geom_pointrange() x, y, ymin, ymax, alpha, color, fill, group, linetype, shape, size</p>
<p>One Variable</p> <p>Continuous c <- ggplot(mpg, aes(hwy)); c2 <- ggplot(mpg)</p> <p>c + geom_area(stat = "bin") x, y, alpha, color, fill, linetype, size</p> <p>c + geom_density(kernel = "gaussian") x, y, alpha, color, fill, group, linetype, size, weight</p> <p>c + geom_dotplot() x, y, alpha, color, fill</p> <p>c + geom_freqpoly() x, y, alpha, color, group, linetype, size</p> <p>c + geom_histogram(binwidth = 5) x, y, alpha, color, fill, linetype, size, weight</p> <p>c2 + geom_qq(aes(sample = hwy)) x, y, alpha, color, fill, linetype, size, weight</p> <p>Discrete d <- ggplot(mpg, aes(fill))</p> <p>d + geom_bar() x, alpha, color, fill, linetype, size, weight</p>	<p>Discrete X, Continuous Y f <- ggplot(mpg, aes(class, hwy))</p> <p>f + geom_col() x, y, alpha, color, fill, group, linetype, size</p> <p>f + geom_boxplot() x, y, lower, middle, upper, ymax, ymin, alpha, color, fill, group, linetype, shape, size, weight</p> <p>f + geom_dotplot(binaxis = "y", stackdir = "center") x, y, alpha, color, fill, group</p> <p>f + geom_violin(scale = "area") x, y, alpha, color, fill, group, linetype, size, weight</p> <p>Discrete X, Discrete Y g <- ggplot(diamonds, aes(cut, color))</p> <p>g + geom_count() x, y, alpha, color, fill, shape, size, stroke</p>
	<p>Maps data <- data.frame(murder = USArrests\$Murder, state = tolower(rownames(USArrests))) map <- map_data("state") k <- ggplot(data, aes(fill = murder))</p> <p>k + geom_map(aes(map_id = state), map = map) + expand_limits(x = map\$long, y = map\$lat) map_id, alpha, color, fill, linetype, size</p>
	<p>Three Variables</p> <p>seals\$z <- with(seals, sqrt(delta_long^2 + delta_lat^2)) l <- ggplot(seals, aes(long, lat))</p> <p>l + geom_raster(aes(fill = z), hjust = 0.5, vjust = 0.5, interpolate = FALSE) x, y, alpha, fill</p> <p>l + geom_contour(aes(z = z)) x, y, z, alpha, colour, group, linetype, size, weight</p> <p>l + geom_tile(aes(fill = z)) x, y, alpha, color, fill, linetype, size, width</p>



Example

```
data <- data.frame(  
  type = c( rep("variable 1", 1000), rep("variable 2", 1000) ),  
  value = c( rnorm(1000), rnorm(1000, mean=4) ) ) # Represent it
```

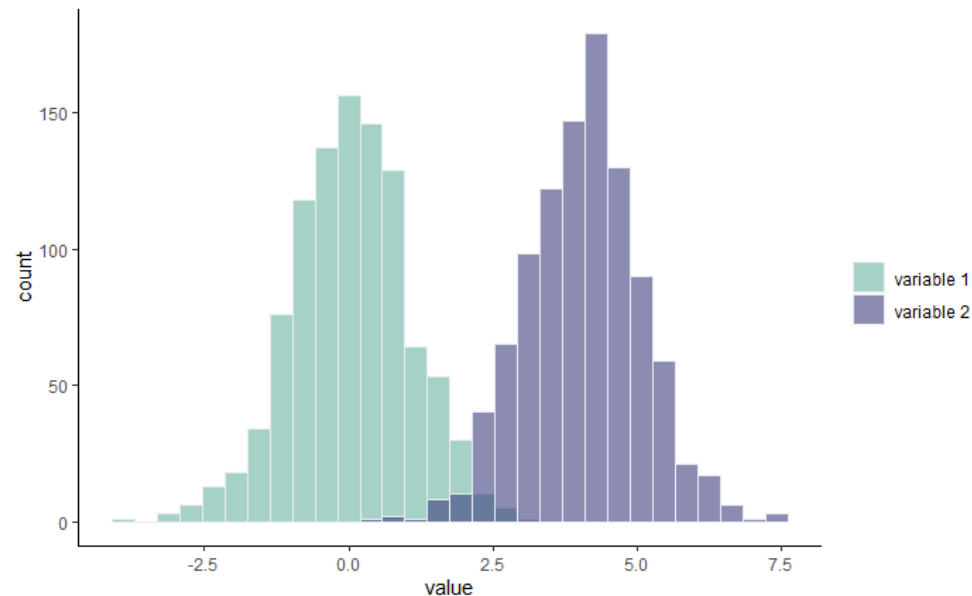
```
ggplot(data, aes(x=value, fill=type)) +  
  geom_histogram( color="#e9ecef", alpha=0.6, position = 'identity') +  
  scale_fill_manual(values=c("#69b3a2", "#404080")) + theme_classic()  
+ labs(fill="")
```



1. Generate a dataframe with two variables and 1000 observations
2. Generate random values based on a normal distribution

Example

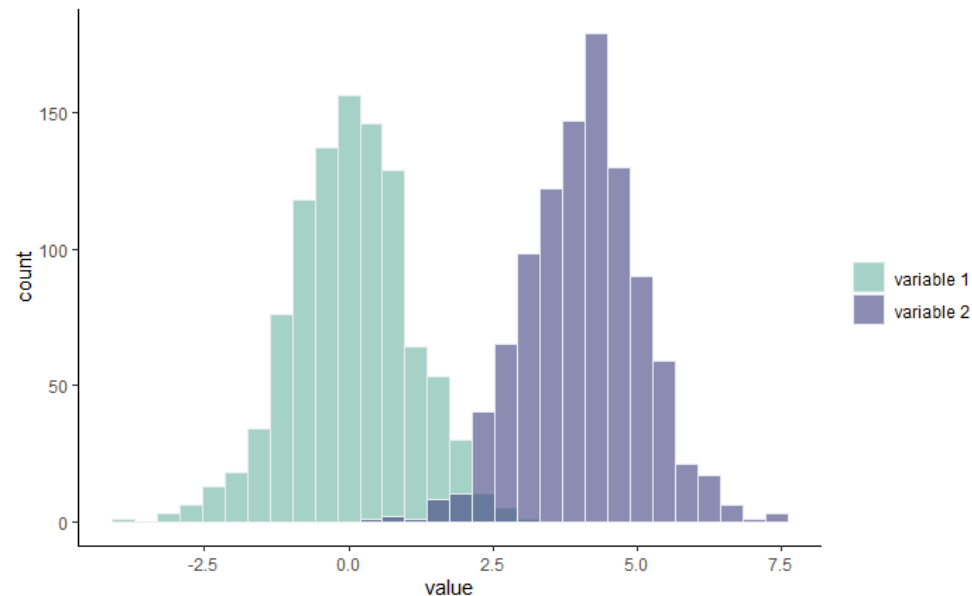
```
data <- data.frame(  
  type = c( rep("variable 1", 1000), rep("variable 2", 1000) ),  
  value = c( rnorm(1000), rnorm(1000, mean=4) ) ) # Represent it  
  
ggplot(data, aes(x=value, fill=type)) +  
  geom_histogram( color="#e9ecef", alpha=0.6, position = 'identity') +  
  scale_fill_manual(values=c("#69b3a2", "#404080")) + theme_classic()  
  + labs(fill="")
```



1. Generate a dataframe with two variables and 1000 observations
2. Generate random values based on a normal distribution
3. Select the data and variables we want to plot

Example

```
data <- data.frame(  
  type = c( rep("variable 1", 1000), rep("variable 2", 1000) ),  
  value = c( rnorm(1000), rnorm(1000, mean=4) ) ) # Represent it  
  
ggplot(data, aes(x=value, fill=type)) +  
  geom_histogram( color="#e9ecef", alpha=0.6, position = 'identity') +  
  scale_fill_manual(values=c("#69b3a2", "#404080")) + theme_classic()  
  + labs(fill="")
```

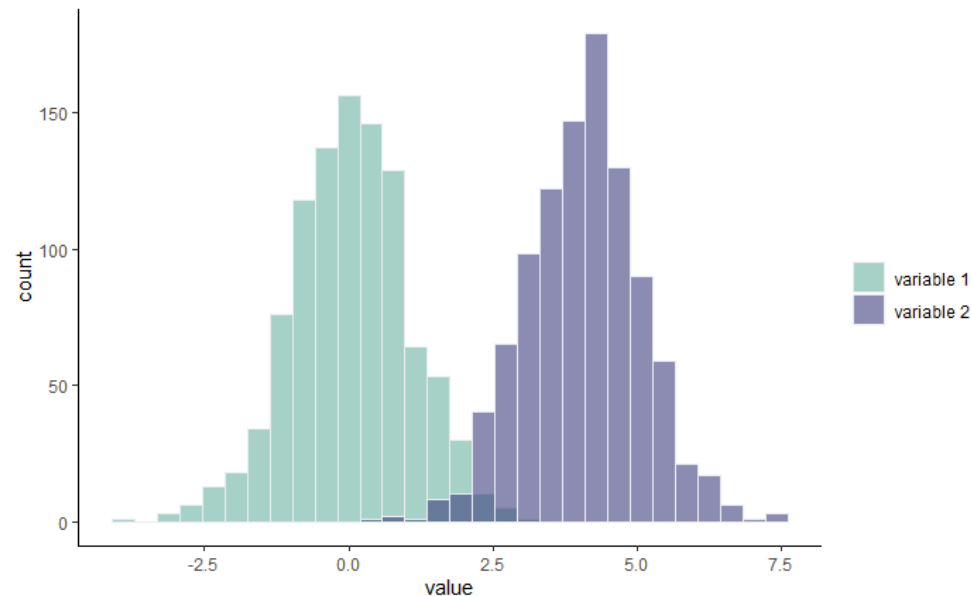


1. Generate a dataframe with two variables and 1000 observations
2. Generate random values based on a normal distribution
3. Select the data and variables we want to plot
4. Select the type of visualization, identify, color sets the lines, alpha for transparency and identify overlaps the bar

Example

```
data <- data.frame(
  type = c( rep("variable 1", 1000), rep("variable 2", 1000) ),
  value = c( rnorm(1000), rnorm(1000, mean=4) ) ) # Represent it

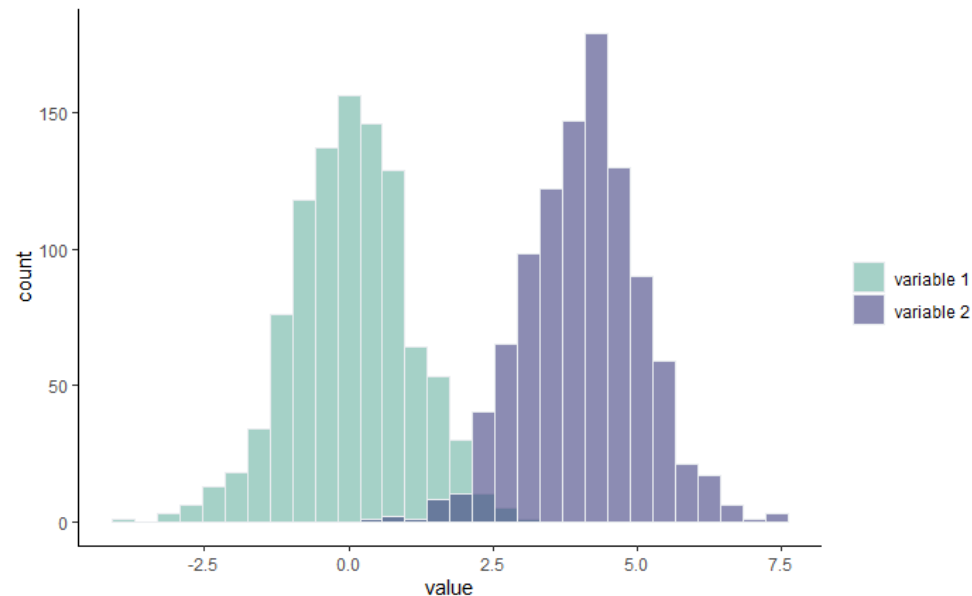
ggplot(data, aes(x=value, fill=type)) +
  geom_histogram( color="#e9ecef", alpha=0.6, position = 'identity') +
  scale_fill_manual(values=c("#69b3a2", "#404080")) + theme_classic()
+ labs(fill="")
```



1. Generate a dataframe with two variables and 1000 observations
2. Generate random values based on a normal distribution
3. Select the data and variables we want to plot
4. Select the type of visualization, identify, color sets the lines, alpha for transparency and identify overlaps the bar
5. We fill each histogram with a different colour

Example

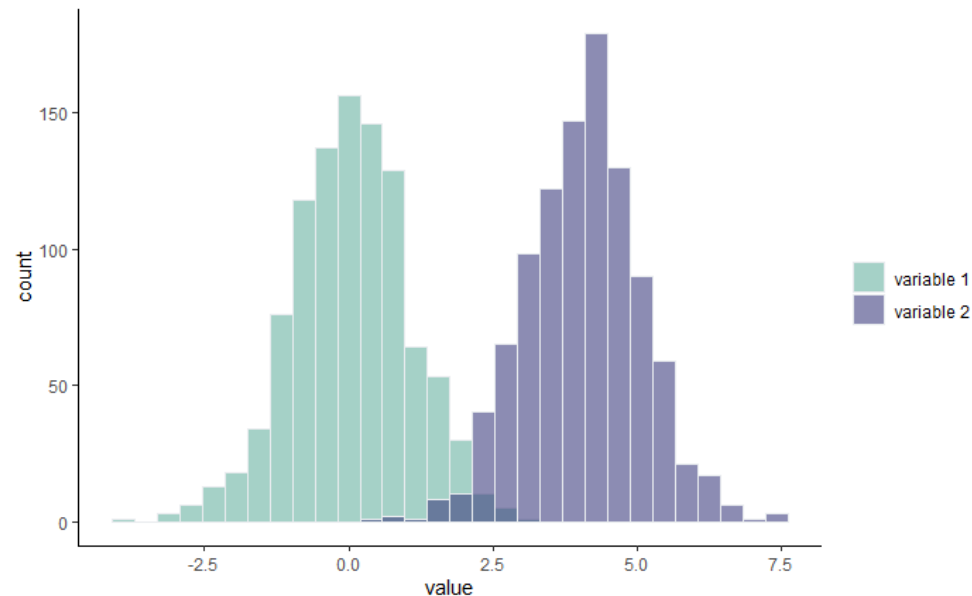
```
data <- data.frame(  
  type = c( rep("variable 1", 1000), rep("variable 2", 1000) ),  
  value = c( rnorm(1000), rnorm(1000, mean=4) ) ) # Represent it  
  
ggplot(data, aes(x=value, fill=type)) +  
  geom_histogram( color="#e9ecef", alpha=0.6, position = 'identity') +  
  scale_fill_manual(values=c("#69b3a2", "#404080")) + theme classic()  
  + labs(fill="")
```



1. Generate a dataframe with two variables and 1000 observations
2. Generate random values based on a normal distribution
3. Select the data and variables we want to plot
4. Select the type of visualization, identify, color sets the lines, alpha for transparency and identify overlaps the bar
5. We fill each histogram with a different colour
6. Choose a preset theme

Example

```
data <- data.frame(  
  type = c( rep("variable 1", 1000), rep("variable 2", 1000) ),  
  value = c( rnorm(1000), rnorm(1000, mean=4) ) ) # Represent it  
  
ggplot(data, aes(x=value, fill=type)) +  
  geom_histogram( color="#e9ecef", alpha=0.6, position = 'identity') +  
  scale_fill_manual(values=c("#69b3a2", "#404080")) + theme_classic()  
+ labs(fill="")
```



1. Generate a dataframe with two variables and 1000 observations
2. Generate random values based on a normal distribution
3. Select the data and variables we want to plot
4. Select the type of visualization, identify, color sets the lines, alpha for transparency and identify overlaps the bar
5. We fill each histogram with a different colour
6. Choose a preset theme
7. Names for labs added

$$\mathbf{x} = \mathbf{x}_f - \mathbf{x}_i \quad \Delta \mathbf{v} = \mathbf{v}_f - \mathbf{v}_i$$

$$= \frac{\Delta \vec{r}}{\Delta t} \quad \vec{a} = \frac{\Delta \vec{v}}{\Delta t}$$

$$v = |\mathbf{v}| = \sqrt{v_x^2 + v_y^2}$$

$$\theta = \tan^{-1}\left(\frac{v_y}{v_x}\right)$$



$$\omega = \frac{\Delta \theta}{\Delta t} \quad \alpha = \frac{\Delta \omega}{\Delta t}$$

$$= \mathbf{v}_0 + \mathbf{a}t$$

$$= \mathbf{x}_0 + \mathbf{v}_0 t + \frac{1}{2} \mathbf{a}t^2$$

$$-v_o^2 = 2a(x - x_o)$$

$$= \frac{v_f^2 + v_i^2}{2}$$

Data Visualization

$$\omega = 2\pi f \quad f = \frac{1}{T}$$

$$\omega = \omega_0 + \alpha t$$

$$\theta = \theta_0 + \omega_0 t + \frac{1}{2} \alpha t^2$$

$$\omega_o^2 = 2\alpha(\theta - \theta_o)$$

Curvefit Rankings for 0.5% SEV CO₂

Rank	F-statistic
1	7.962883557
2	7.8601110639
3	7.5283512645
4	7.3357010958
5	6.3801158367
6	3.8079206858
7	3.742891358
8	3.5727028219
9	3.5546937052
10	3.0133372321
11	2.7408796673
12	2.6986270263
13	2.5801276758
14	2.5622800357
15	2.1798855221

Prof. Dr. Javier Valdes
Javier.valdes@th-deg.de

IAI - Institut für Angewandte Informatik
 Institute for Applied Informatics

Technische Hochschule Deggendorf
 Technologie Campus Freyung
 Grafenauer Str. 22, D- 94078 Freyung,
 Germany

Tel.: +49 8551 91764 40
 Fax: +49 8551 91764 69

$$x = A \cos(\omega t + \phi) \quad v = -A \omega \sin(\omega t + \phi)$$